

# The Future of Australian Mortality

Heather Booth  
Rajesh Chauhan  
John Maindonald  
Len Smith

Australian National University

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# Background

- Lee and Carter (1992): USA
- Tuljapurkar et al (2000): G7 countries
- ABS projections 1999-2101

# Lee and Carter: method

- No subjective judgements involved
- Based on past mortality rates

# The model

$$\ln(m_{x,t}) = a_x + b_x k_t + \varepsilon_{x,t} \dots \dots \dots (1)$$

- $\ln(m_{x,t})$  is a matrix of log age specific death rates
- $k_t$  is the index of improvement in mortality over time ('dominant temporal signal')
- $a_x$  and  $b_x$  are the age specific constants; indicate the rate of decline in specific age group
- $\varepsilon_{x,t}$  is the error term of the equation with mean 0 and variance  $\sigma_\varepsilon^2$

# Data adjustment

- Adjust data prior to fitting the model
- Extension to age 105+
  - relational logistic model fitted to ages 50 to 85+ (Himes, Preston & Condran 1994)
- Normalisation
  - adjust  $\ln[m(x,t)]$  by subtracting the mean over time of  $\ln[m(x,t)]$

# Singular Value Decomposition

- Solution found by SVD method
- First left and right vectors and leading value of SVD provide a unique solution:
  - dominant temporal signal,  $k(t)$
  - fixed relative age effects,  $b(x)$

# Singular Value Decomposition

$$X = TDA'$$

Where:

**X** is the matrix of normalised log death rates

**T** is the matrix of time effect vectors

**A** is the matrix of age effect vectors

**D** is the diagonal matrix of singular values

# ARIMA fit

- ARIMA (auto-regressive integrated moving average) used to project future signal
- Random walk with drift,  $z$
- $\hat{k}(t+1) = \hat{k}(t) - z + \varepsilon_t$
- Fitted to  $k$  1950-1994
- Projected  $k$  1995-2050
- Confidence limits of projection estimated from error of fit

# Lee and Carter: application

- US 1900-1989; projected to 2065
- Life expectancy  $>$  official projections
- Adopted widely in North America

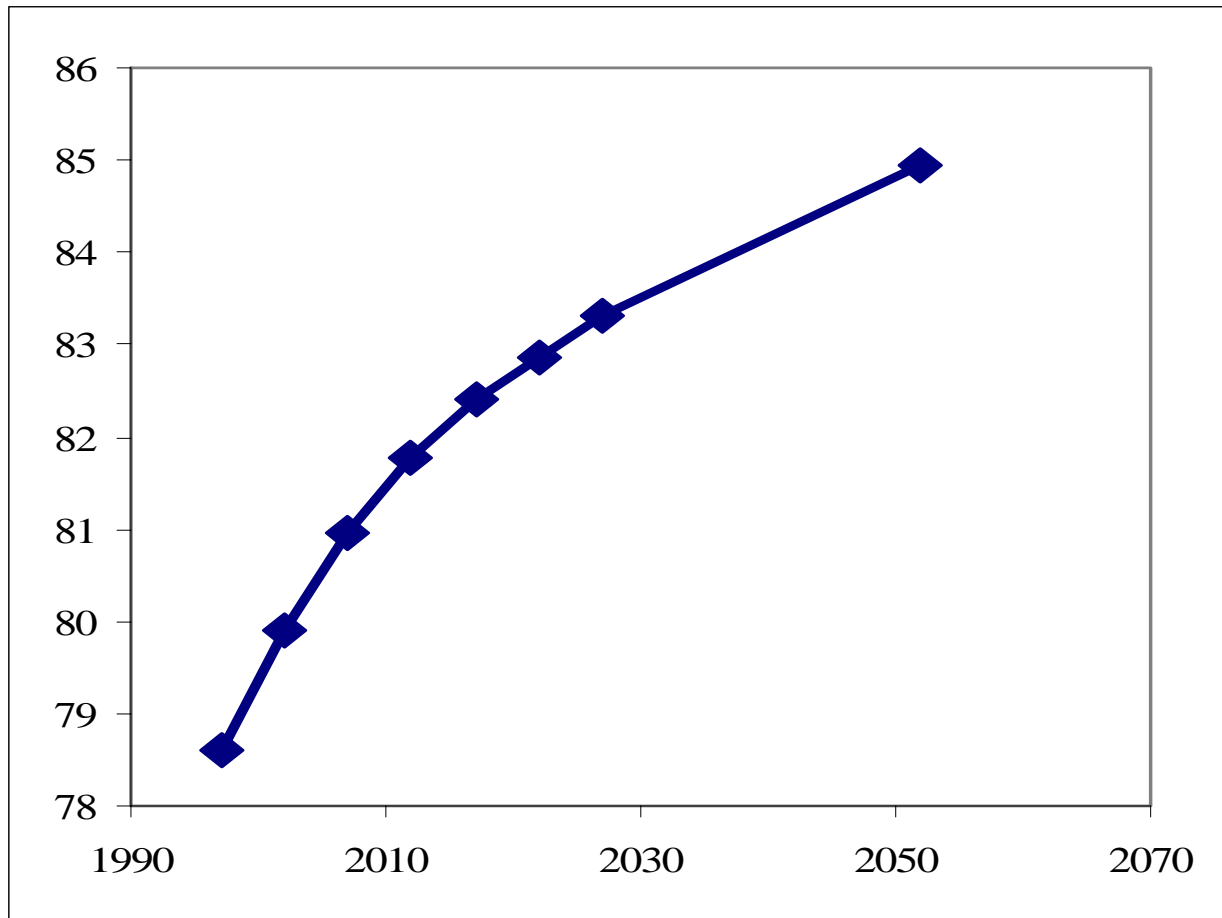
# Tuljapurkar et al: application

- G7 countries: Canada, France, Germany, Italy, Japan, UK, US
- 1950-1994 data; projected to 2050
- ‘Universal’ pattern: exponential decline at all ages
- $e(0) < \text{official}$  in short term, but  $> \text{official}$  in long term

# ABS projections 1999-2101

- First period 1997-2002
  - increase of 0.30 per annum in male  $e(0)$
  - increase of 0.22 per annum in female  $e(0)$
- Declining rate of increase thereafter
- By 2051
  - male  $e(0) = 83.3$  years
  - female  $e(0) = 86.6$  years
- past age pattern of change to 2027

# ABS projected $e(0)$ 1997-2052



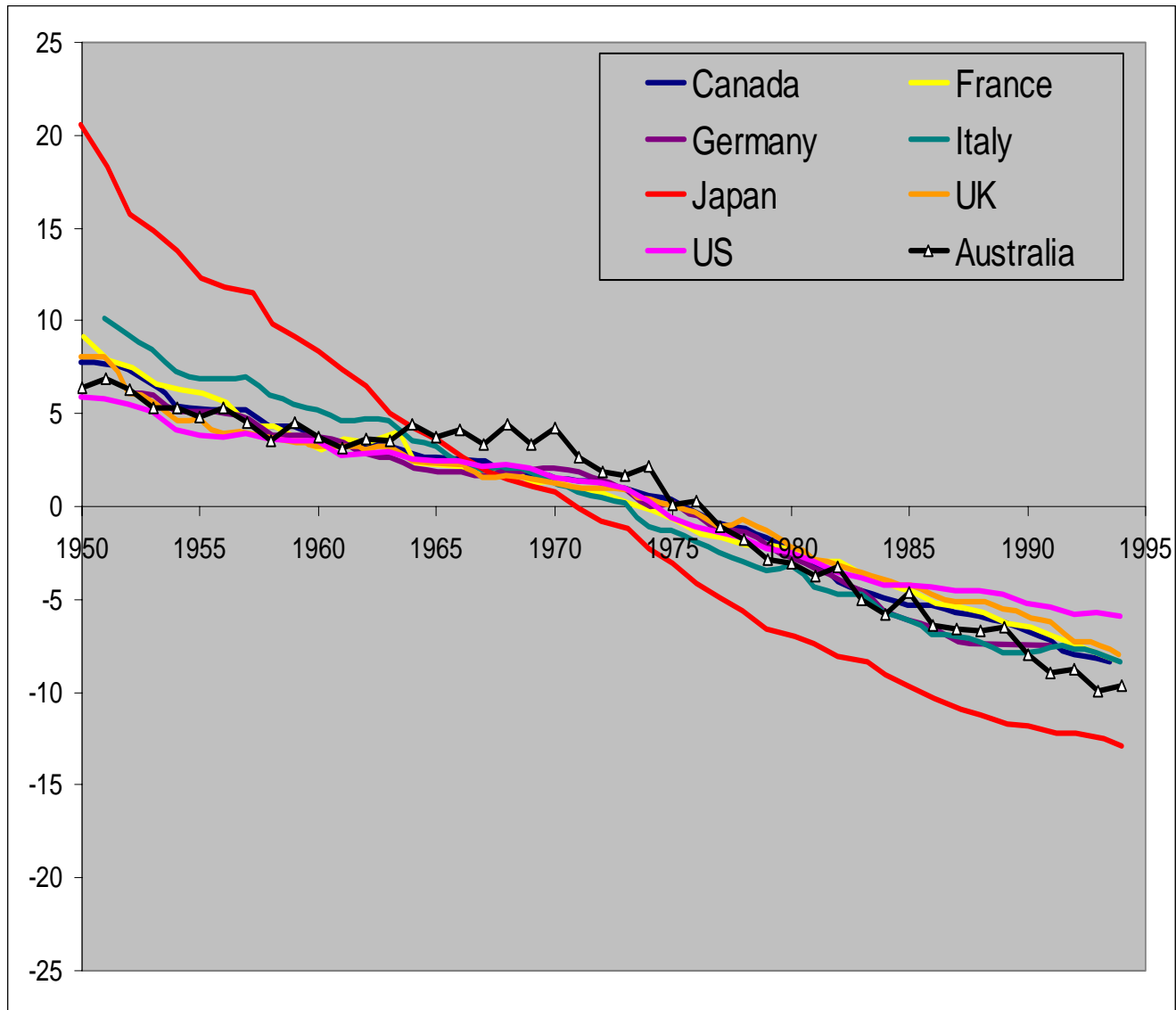
# The Australian study

- Apply Lee-Carter method to Australian data following Tuljapurkar et al.
- Compare Australia with G7 analysis
- Compare new projections with ABS projections, 1999-2050

# Results

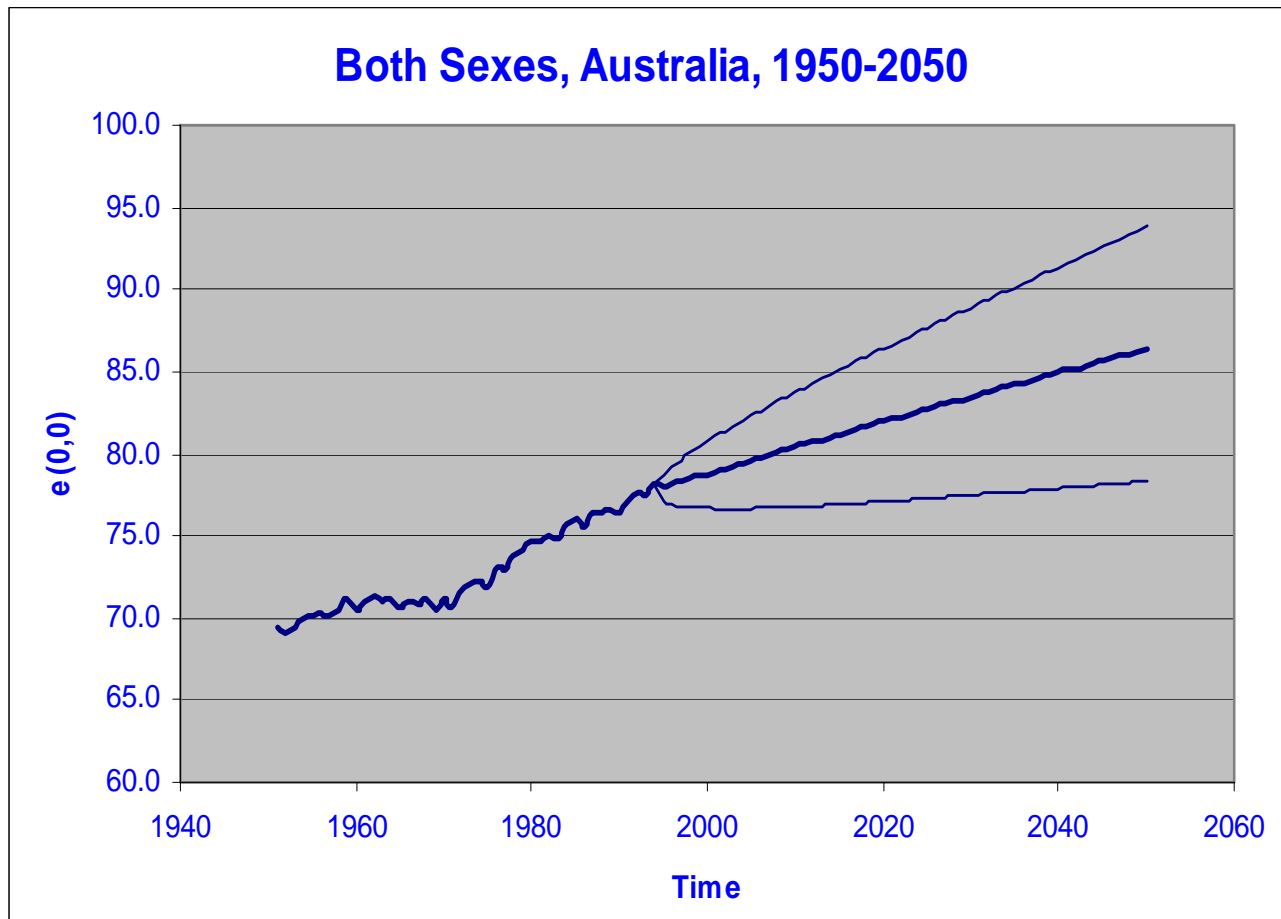
- 95 per cent of variance explained by first vectors and value of SVD

# Values of $k$ : G7 + Australia





# Observed and projected $e(0)$



# Discussion

- Differences between Australia and other countries
- Differences between Lee-Carter and official projections
- Further research:
  - by sex, by cause, by cohort
  - limits to life expectancy
  - improvements in methodology

# Comparison of ABS and L-C $e(0)$

